

## OPTIMAL REGULATION OF CREDIT LINES

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The views presented here do not necessarily represent those of the Bank of Spain or the Eurosystem.



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- ⇒ This paper provides a normative analysis of CLs

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- ▶ Parties optimally agree on the CL contractual terms (prices + pre-arranged funding)

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3. I discuss the implementation of the constrained-efficient allocation
  - It can be implemented using a minimum requirement on pre-arranged funding
4. I examine the main determinants of the regulatory requirement
  - It should go up when the costs of maintaining liquidity buffers are lower, the costs of liquidating firms are higher, or high liquidity need states occur more frequently

## OUTLINE

1. Introduction
2. Model
3. Equilibrium Analysis
4. Social welfare analysis
5. Conclusions



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- 2. **Banks** channel funds from investors to firms by means of CLs
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- 3. **Investors** demand  $R + \delta$  ( $\delta \geq 0$ ) and  $R > 1$  at date 2 for  $E$  and  $D$ , respectively

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- ▶ Aggregate uncertainty
  - $\alpha \sim g(\cdot)$  is publicly revealed at  $t = 1$
  - $g(\cdot)$  is known when contracting at  $t = 0$

- ▶ At  $t = 2$ , the firm produces a cash flow

$$\tilde{x} = \begin{cases} X, & \text{if not liquidated,} \\ Q(z), & \text{if liquidated,} \end{cases}$$

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- ▶ Payoffs can be derived from a model of debt overhang w/ a secondary market for specialized assets

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- ▶ Contractual terms  $B, f$ , and  $E$  are determined by competition at  $t = 0$

- ▶ In high liquidity need states,  $\alpha$  may be unfeasible to meet:  $D < \alpha - E$ 
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- ▶ (Junior) pre-arranged funding  $E$  helps to sustain lending over a wider range of  $\alpha$ 's
  - Claims associated to  $E$  can be diluted to raise additional funds at  $t = 1$
  - Yet, pre-arranged funding  $E$  demands a higher return

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(+) Symmetric eq. can fully characterize the unregulated CL  $(B^U, f^U, E^U)$

Given aggregate liquidations  $z(\alpha)$ , the representative bank maximizes

$$\max_{B, f, E} \int_0^{\alpha} \left( (1-\alpha)(X-f) + \alpha(X-B) \right) g(\alpha) d\alpha + \int_{\underline{\alpha}}^1 \left( (1-\alpha)(X-f) + \alpha \left( \frac{L}{\alpha}(X-B) + \left(1 - \frac{L}{\alpha}\right) Q(z) \right) \right) g(\alpha) d\alpha,$$

subject to the initial investors' participation constraint

$$(R + \delta)E = \int_0^{\alpha} (\alpha B + (1 - \alpha)f - R(\alpha - E)) g(\alpha) d\alpha. \quad (\text{PC})$$

Def.: Equilibrium

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- ▶ Are liquidations in high liquidity need states due to partial insurance efficient?

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## The social planner's problem:

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- ▶ Contractual terms are chosen to equalize marginal social benefit to marginal social cost of  $E$
- ▶ Socially desirable to increase  $E > E^U$

Appendix 1

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Appendix 2

- High requirements can make CLs excessively costly
- Low requirements can have null impact on welfare

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# Appendix

It consists of a choice  $(B^U, f^U, E^U)$  for the representative bank and aggregate liquidations  $z^U(\alpha)$  such that

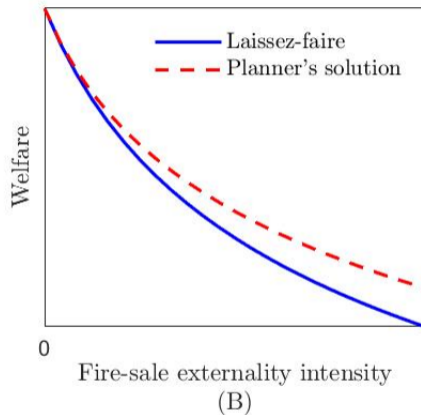
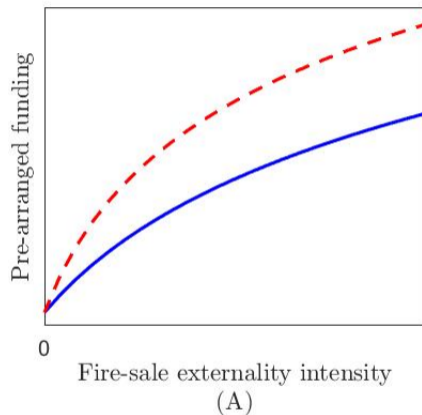
1. Given  $z^U(\alpha)$ ,  $(B^U, f^U, E^U)$  solves the bank's optimization problem, that is,

$$\max_{B, f, E} V(B, f, E)$$

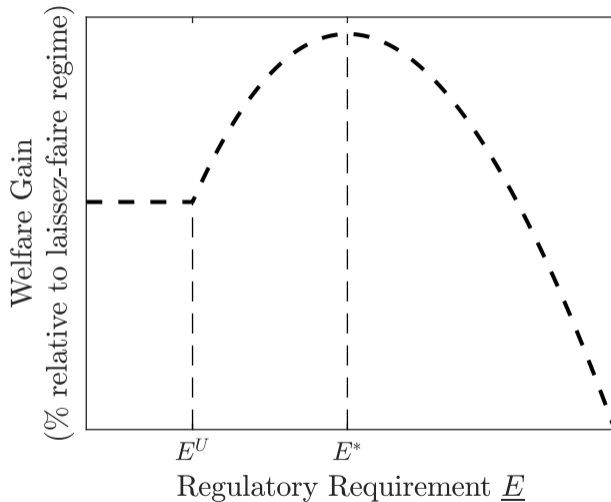
subject to the participation constraint (PC) of initial investors.

2. Given  $(B^U, f^U, E^U)$ , aggregate liquidations are computed as  $z^U(\alpha) = \alpha - L \quad \forall \alpha$ , where

$$L = \begin{cases} \alpha, & \text{if } \alpha \leq \underline{\alpha}, \\ \frac{RE^U + (1 - \alpha)f^U}{R - B^U}, & \text{if } \alpha > \underline{\alpha}. \end{cases}$$



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